

Chapter 21

Coulomb's Law

→ Electric Charge :

2 kinds of Charges

- positive Charge
- Negative Charge

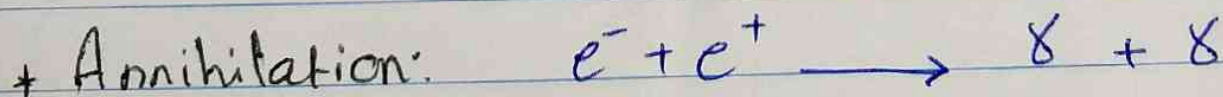
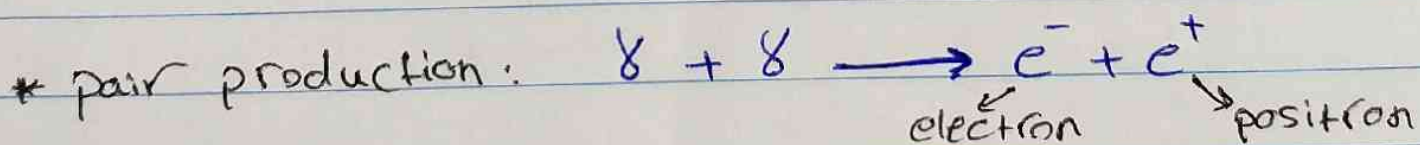
□ □ Quantization of Charge:-

$$* q = ne, \quad n = \pm 1, \pm 2, \pm 3, \dots$$

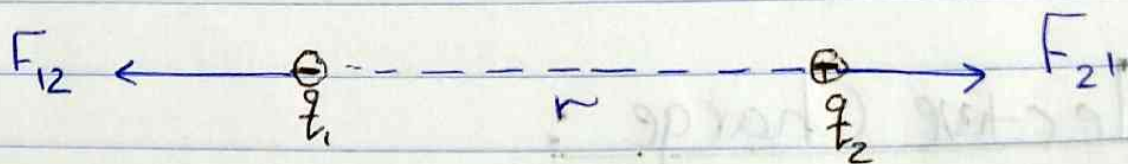
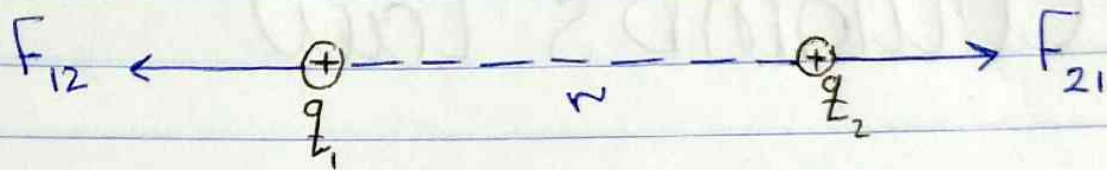
$$* \text{electron charge} = e = -1.6 \times 10^{-19} \text{ C}$$

□ Conservation of Charge:-

$$q_{\text{before reaction}} = q_{\text{after reaction}}$$

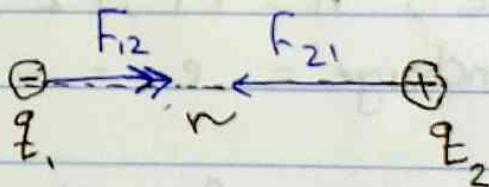


→ Electric force:



* The electric force between similar charges are electric repulsive force.

* The electric force between opposite charges are electric attractive force



* $F_{12} = -F_{21}$ ("depend on F as a vector")

* $F_{12} = F_{21}$ ("depend on F as a magnitude")

→ Coulomb's law:-

$$F \propto \frac{q_1 q_2}{r^2}$$

* Electric force directly proportional with q_1, q_2

* Electric force inversely proportional with r^2 .

$$F = \frac{k q_1 q_2}{r^2}$$

- k : constant depend on a. Units
b. medium between q_1 & q_2 .

• ϵ : permittivity of the medium.

• In air: $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N}\cdot\text{m}^2$

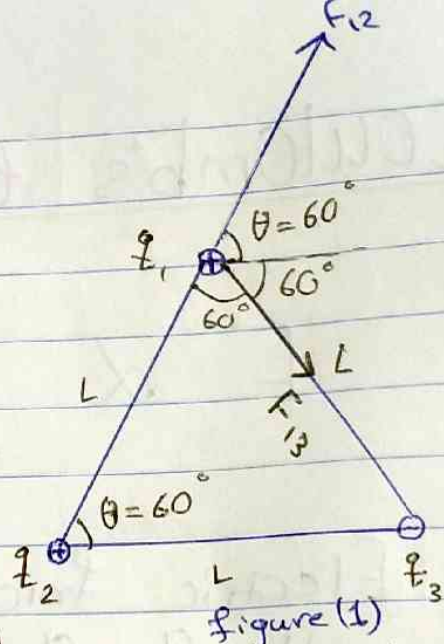
• $k = \frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$.

Example:

$$q_1 = q_2 = 50 \mu\text{C}$$

$$q_3 = -50 \mu\text{C}$$

$$L_{12} = L_{23} = L_{13} = 50 \text{ cm}$$



* find the net force On q_1 ?
or
resultant force

$$F = \frac{9 \times 10^9 \times q_1 \times q_2}{r^2}$$

$$F_{12} = \frac{9 \times 10^9 \times 50 \times 10^{-6} \times 50 \times 10^{-6}}{(0.5)^2}$$

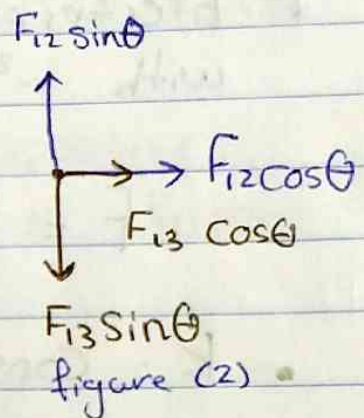
= 90 N In the direction shown in figure (1)

$$F_{13} = \frac{9 \times 10^9 \times 50 \times 10^{-6} \times 50 \times 10^{-6}}{(0.5)^2}$$

= 90 N In the direction shown in figure (2)

$$\bullet F_y = F_{12} \sin 60 - F_{13} \sin 60 = 0$$

$$\bullet F_x = F_{12} \cos 60 + F_{13} \cos 60 = 90 \cos 60 + 90 \cos 60$$
$$= 90 \text{ N in } (+x) \text{ direction}$$
$$= \text{or } 90 \text{ N } \hat{i}$$



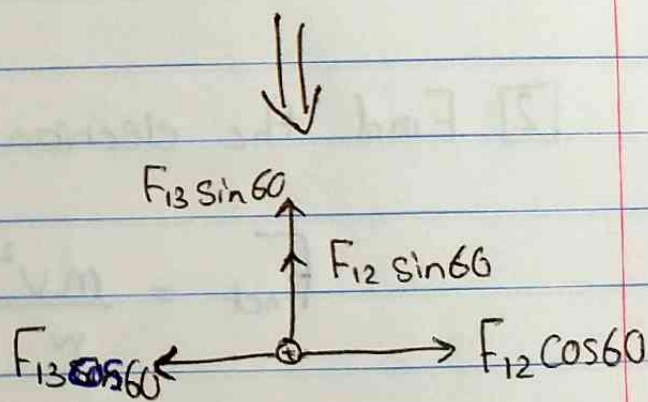
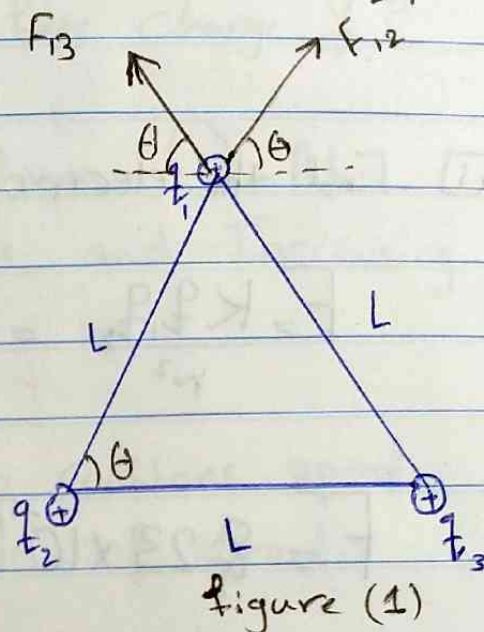
Example:

- let $q_3 = +50 \mu\text{C}$

⇒ Find the resultant (electrostatic) force on q_1 !

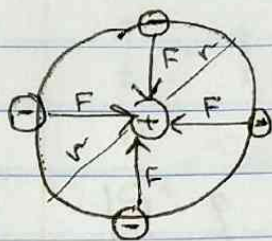
$$\begin{aligned} F_y &= F_{12} \sin 60 + F_{13} \sin 60 \\ &= 90 \frac{\sqrt{3}}{2} + 90 \frac{\sqrt{3}}{2} \\ &= 156 \text{ N}^2 \text{ in } (+y) \text{ direction} \\ &= \text{or } 156 \uparrow \text{ N} \end{aligned}$$

$$\begin{aligned} F_x &= F_{12} \cos 60 - F_{13} \cos 60 \\ &= \text{zero} \end{aligned}$$



Problem:

H. atomic In Bohr's model electron moves in a circular motion around the nucleus (proton).



$$\text{The Radius} = 5.29 \times 10^{-11} \text{ m}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$m_e = 9.11 \times 10^{-31} \text{ kg}$$

[1] Find the electron static force on the electron?

$$F = \frac{k q_1 q_2}{r^2} = \frac{k q_e q_p}{r^2} = \frac{9 \times 10^9 \times 1.6 \times 10^{-19} \times 1.6 \times 10^{-19}}{(5.29 \times 10^{-11})^2}$$

$$F = 8.23 \times 10^{-18}, \text{ toward the Center.}$$

[2] Find the electron speed?

$$F_{\text{net}} = \frac{mv^2}{r} \Rightarrow 8.23 \times 10^{-18} = \frac{9.11 \times 10^{-31} V^2}{5.29 \times 10^{-11}}$$

$$V = 2.187 \times 10^6 \text{ m/s}$$

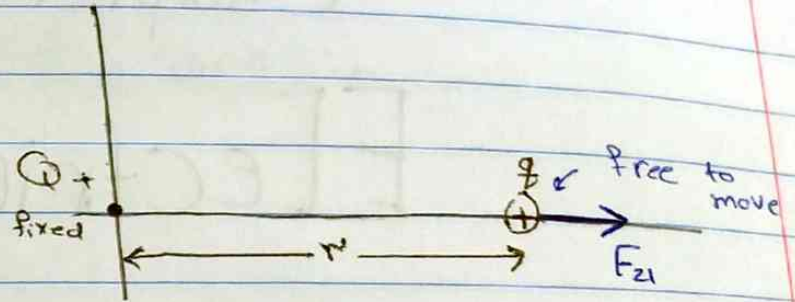
[3] Find the electron kinetic energy?

$$K = \frac{1}{2} m v^2$$

$$= \frac{1}{2} \times 9.11 \times 10^{-31} \times (2.187 \times 10^6)^2$$

$$= 2.18 \times 10^{-18} \text{ J}$$

problem \Rightarrow



1 Describe the motion of free charge q ?

- It will move away from Q At decreasing acceleration and Increasing speed.

- In ∞ it will move in a constant speed with maximum magnitude of speed.